# CS448f: Image Processing For Photography and Vision 

## Deconvolution

## Assignment 3

- Competition
- Lessons Learned


## Project

- Proposals due Thursday
- Everyone should have a pretty good idea of what they plan to do at this stage
- Presentations begin next Tuesday
- Schedule?


## Problems in Photography

|  | Linear Filters | Non-Linear Filters | Alignment | Wavelets | Gradient Domain |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Misfocus or Lens Blur | Sharpening | Sharpening | Focal Stacks Panoramas | Sharpening | ? |
| Motion Blur | Sharpening | Sharpening | ? | ? | ? |
| Noise | Blurring | Bilateral <br> Nonlocal Means | Aligned Averaging | Wavelet Shrinkage | ? |
| Dynamic Range | ? | ToneMapping | HDR <br> Acquisition | ? | ToneMapping |
| Composition | Multi-Band Blending | ? | Panoramas | ? | Poisson Blending |

## Problems in Photography

|  | Linear <br> Filters | Non-Linear Filters | Alignment | Wavelets | Gradient Domain | Deconvolution |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Misfocus or Lens Blur | Sharpening | Sharpening | Focal Stacks Panoramas | Sharpening | ? | $\sqrt{ }$ |
| Motion Blur | Sharpening | Sharpening | ? | ? | ? | $\sqrt{ }$ |
| Noise | Blurring | Bilateral Nonlocal Means | Aligned Averaging | Wavelet <br> Shrinkage | ? | X |
| Dynamic Range | ? | Tone- <br> Mapping | HDR <br> Acquisition | ? | ToneMapping | ? |
| Composition | Multi-Band Blending | ? | Panoramas | ? | Poisson Blending | ? |

Motion Blur (Handheld 200mm 1/50 s)


Motion Blur (Handheld 200mm, 1/50s)

## Less Motion Blur (1/640s)



## Motion Blur = Convolution



## Convolution = Linear Operator

- Image * kernel = blurry
- $\mathrm{Km}=\mathrm{b}$
$-K=$ the blur (may or may not be known)
$-m=$ the unknown good image
$-b=$ the known blurry image
- K is known = nonblind deconvolution
- K is unknown = blind deconvolution


## Estimating K

- Include an accelerometer
- Look for the path traced by bright points
- Bounce back and forth between estimating K and estimating m
- Deconvolution using Natural Image Priors
- Levin et al. 2007


## Deconvolution = Least Squares

- Assuming we know K
- Find m such that $\mathrm{Km}=\mathrm{b}$
- Alternatively, minimize $(\mathrm{Km}-\mathrm{b})^{2}$


## Solution Methods: Input

## Solution Methods: Gradient Descent



## Solution Methods: Richardson-Lucy

## Solution Methods: Richardson-Lucy

- $\mathrm{m} *=\mathrm{K}^{\top}(\mathrm{b} /(\mathrm{Km}))$
- Like a multiplicative gradient descent
- Each step conserves average brightness in each region
- ImageStack -load blurry.tmp -loop --dup --load kernel.tmp --pull 1 --convolve --pull 1 --pop -load blurry.tmp --divide --load kernel.tmp --flip x --flip y --pull 1 --convolve --pull 1 --pop -multiply --save rl.tmp --display


## High-Frequency Junk



## Priors

- The result image above satisfies the equation:
$-\mathrm{Km}=\mathrm{b}$
- Why does it look bad?


## Priors

- The result image above satisfies the equation:
$-\mathrm{Km}=\mathrm{b}$
- Why does it look bad?
- There's extra high-frequency junk


## Gradient Magnitude



Original
Richardson Lucy Result

## Gradient Magnitude



Original
Richardson Lucy Result

## Let's also minimize gradients

- $\mathrm{Km}=\mathrm{b}$
- $D_{x} m=0$
- $D_{y} m=0$
- Solving this least-squares minimizes:
$|K m-b|^{2}+\left|D_{x} m\right|^{2}+\left|D_{y} m\right|^{2}$
= L2-norm of error + L2-norm of gradient field


## Let $\mathrm{m}=$ correct answer



## Let $\mathrm{m}=$ Richardson Lucy

$|K m-b|^{2}$
$\left|D_{x} m\right|^{2}+\left|D_{y} m\right|^{2}$

## Let $\mathrm{m}=$ blurry input


$|K m-b|^{2}$
$\left|D_{x} m\right|^{2}+\left|D_{y} m\right|^{2}$

## Gradient Magnitude is a Bad Prior

- It strongly prefers blurry output if at all possible
- The prior and the error fight each other
- What's a better prior?


## Strong Gradients are Sparse



## Strong Gradients are Sparse

## Our old prior:



Original Grad ${ }^{\wedge} 2$


Motion-Blurred Grad ^ 2

# Slightly better to count the number of large edges, and minimize that 



Original Grad ^ 0.125
Motion-Blurred Grad ^ 0.125

## Given a black-white transition...

Sum of gradients raised to power < 1 prefers sharp edges:

Sum of gradients raised to power > 1 prefers smooth edges:

## Optimization

- Solving this least-squares minimizes: $-|K m-b|^{2}+\left|D_{x} m\right|^{2}+\left|D_{y} m\right|^{2}$
- We want to minimize something like this: $-|K m-b|^{2}+\left|D_{x} m\right|^{1 / 2}+\left|D_{y} m\right|^{1 / 2}$
- No longer a convex optimization problem...
- Can still use gradient descent to find a local minima
- it picks a sensible looking place for each edge


## Some results

- http://graphics.ucsd.edu/~neel/dissertation/chapter5results/


## More Fun in the Gradient Domain

- So if gradients should be sparse, and we see a gradient that looks like this:

| 0 | 0 | 1 | 3 | 5 | 6 | 4 | 1 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

- Why not convert it to this:

| 0 | 0 | 1 | 3 | 5 | 6 | 4 | 1 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 1 | 3 | 15 | 1 | 0 | 0 | 0 |

## More Fun in the Gradient Domain

- If it works: call it deblurring
- If it doesn't: call it a "painterly effect"



